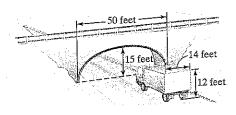
## Conic Sections

9. 
$$x^2 + y^2 - 4x + 2y - 4 = 0$$
  
10.  $x^2 + y^2 - 4y = 0$ 

10.2 In Exercises 11–16, graph each ellipse.

17. A semielliptic archway has a height of 15 feet at the center and a width of 50 feet, as shown in the figure. The 50-foot width consists of a two-lane road. Can a truck that is 12 feet high and 14 feet wide drive under the archway without going into the other lane?



**10.3** In Exercises 18–21, use vertices and asymptotes to graph each hyperbola.

10.4 In Exercises 22–25, use the vertex and intercepts to sketch the graph of each equation. If needed, find additional points on the parabola by choosing values of y on each side of the axis of symmetry.

the axis of symmetry.  
22. 
$$x = (y - 3)^2 - 4$$
  
24.  $x = y^2 - 8y + 12$   
25.  $x = -2(y + 3)^2 + 2$   
25.  $x = -y^2 - 4y + 6$ 

In Exercises 26–32, indicate whether the graph of each equation is a circle, an ellipse, a hyperbola, or a parabola.

26. 
$$x + 8y = y^2 + 10$$
  
27.  $16x^2 = 32 - y^2$   
28.  $x^2 = 25 + 25y^2$   
29.  $x^2 = 4 - y^2$ 

**32.** 
$$y = x^2 + 6x + 9$$

In Exercises 33–41, indicate whether the graph of each equation is a circle, an ellipse, a hyperbola, or a parabola. Then graph the conic section.

**33.** 
$$5x^2 + 5y^2 = 180$$

**34.** 
$$4x^2 + 9y^2 = 36$$
  
**35.**  $4x^2 - 9y^2 = 36$ 

**36.** 
$$\frac{x^2}{25} + \frac{y^2}{1} = 1$$

**37.** 
$$x + 3 = -y^2 + 2y$$

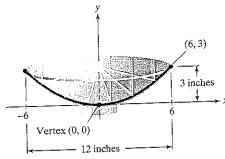
**38.** 
$$y - 3 = x^2 - 2x$$

39. 
$$\frac{(x+2)^2}{16} + \frac{(y-5)^2}{4} = 1$$

40. 
$$(x-3)^2 + (y+2)^2 = 4$$

41. 
$$x^2 + y^2 + 6x - 2y + 6 = 0$$

42. An engineer is designing headlight units for automobiles. The unit has a parabolic surface with a diameter of 12 inches and a depth of 3 inches. The situation is illustrated in the figure, where a coordinate system has been superimposed.



a. Use the point (6, 3) to write an equation in the form  $y = ax^2$  for the parabola used to design the headlight.

b. The light source should be placed at the focus (0, p). The value of p is given by the equation  $a = \frac{1}{4p}$ . Where should the light source be placed? Describe this placement relative to the vertex.

**10.5** In Exercises 43–53, solve each system by the method of your choice.

**43.** 
$$5y = x^2 - 1$$
  $x - y = 1$ 

**44.** 
$$y = x^2 + 2x + 1$$
  
 $x + y = 1$ 

**45.** 
$$x^2 + y^2 = 2$$
  
 $x + y = 0$ 

**46.** 
$$2x^2 + y^2 = 24$$
  
 $x^2 + y^2 = 15$ 

**47.** 
$$xy - 4 = 0$$
  $y - x = 0$ 

**48.** 
$$y^2 = 4x$$
  
 $x - 2y + 3 = 0$ 

**49.** 
$$x^2 + y^2 = 10$$
  $y = x + 2$ 

50. 
$$xy = 1$$
  
 $y = 2x + 1$ 

**51.** 
$$x + y + 1 = 0$$
  
 $x^2 + y^2 + 6y - x = -5$ 

**52.** 
$$x^2 + y^2 = 13$$
  $x^2 - y = 7$ 

**53.** 
$$2x^2 + 3y^2 = 21$$
  
 $3x^2 - 4y^2 = 23$ 

**54.** The perimeter of a rectangle is 26 meters and its area is 40 square meters. Find its dimensions.